The Smoker's problem

A smoker (with a lit cigarette) wishes to walk from the northwest corner of a large gridded network of walkways to the southeast corner. Seated at benches at some of the intersection points are non-smokers. Fearing violence, or showing consideration, the smoker wants to keep as far away from the non-smokers as possible. That is, he aims to find a path whose minimum distance from a non-smoker is as large as possible (the distance between two points in the grid is the sum of their horizontal and vertical separations, and the distance between a point and a path is the minimum distance between the point and any point on the path).

In a further fit of kindness, he also wants to ensure that, subject to meeting the first criterion, the *total* distance between the path and the non-smokers should be as large as possible.

Example

In the grid below non-smokers are marked with dots, and a (not necessarily unique) best path is drawn in red. This is justified as follows – clearly the upper left non-smoker and lower right non-smoker mean the best minimum distance is 2 (and that distance is forced for those two points). The maximum distance we could have for the upper right non-smoker is 6 since we have to cross her horizontal line somewhere. Our first two steps are forced, so the best we could do for the lower left is also 6 - but the third step must reduce the distance to either the upper right or lower left by 1. Choosing a down step, we then succeed in keeping our distance from those two points by the zig zag pattern.



Task

Write a program to find the optimum minimum distance, and also the optimum total distance for that minimum in a sequence of scenarios contained in an input file read in from stdin.

Input format

- Each scenario begins with a line containing the number of horizontal walkways and the number of vertical walkways.
- Each additional line of a scenario describes the locations of the non-smokers (with the upper left at 0 0), increasing from left to right and top to bottom.
- Each scenario is separated from the next by a blank line.

You may assume that there are at most 100 vertical and 100 horizontal walkways, and at most 500 non-smokers in a scenario.

The scenario corresponding to the example above would be:

98

0 8

2 1

6 2

66

Output format

For each scenario print (to stdout) a line of the following form:

min M, total T

where M and T are the largest possible minimum distance achievable and the largest possible total distance achievable for the minimum. So, the output for the scenario above should be

min 2, total 15

Relates to Objectives

1.1 1.2 2.1 2.2 2.3 2.5 2.8 2.9 2.10 3.4 3.5 3.6 4.1 4.2 4.3 4.7 4.8

(3 points, Group)