Visible Surface Determination

Painter's Algorithm
BSP Trees
Z-Buffer
Ray Tracing

## Image or object space

 Ideally an object space method converts the 3D scene into a list of 2D areas to be painted.

 Image space decides for each pixel which surface to paint.

## Image or object space

Painter's Algorithm
BSP Trees
Z-Buffer

Ray Tracing

Hybrid Hybrid Image Object

## **Painter's Algorithm**



# Painter's Algorithm







![](_page_7_Picture_0.jpeg)

![](_page_8_Picture_0.jpeg)

## **Depth Sorting**

Completely in front-put in front
Not overlapping in x, y-either
Intersecting-divide along intersection
overlapping-divide along plane of one polygon.

#### Which side of a plane?

![](_page_10_Figure_1.jpeg)

## **Plane Equation**

(p - n).n = 0p.n - n.n = 0 $\mathbf{p} = (\mathbf{x}, \mathbf{y}, \mathbf{z})$  $\mathbf{n} = (\mathbf{a}, \mathbf{b}, \mathbf{c})$  $ax + by + cz - (a^2 + b^2 + c^2) = 0$ ax + by + cz + d = 0

#### For points p and q

if (p-n).n > 0 and (q-n).n > 0or if (p-n).n < 0 and (q-n).n < 0

p and q are on the same side

![](_page_13_Picture_0.jpeg)

![](_page_14_Picture_0.jpeg)

![](_page_15_Picture_0.jpeg)

#### Divide scene with a plane

 Everything on the same side of that plane as the eye is in front of everything else (from that eye's view)

Divide front and back with more planes
If necessary split polygons by planes

## Efficiency

 BSP trees are order n\*log(n) in the number of polygons

• They are good for VR 'walkthroughs' because you only re-compute traversal when the eye crosses a separating plane

#### **Z-Buffer**

Record r,g,b and z (depth) for each pixel.
Process each polygon line by line and if closer replace r,g,b,z in the buffer.

![](_page_19_Figure_0.jpeg)

## Finding the depth

• Plane equation is Ax + By + Cz + D = 0z = -(Ax + By + D)/C

• replace x by x+1 z' = -(A(x+1) + By + D)/C $\Delta z = z' - z = -A/C$ 

New z is found by adding a constant.

#### What about the lost z?

![](_page_21_Picture_1.jpeg)

 $\equiv (x/z, y/z, 1)$ 

### **Perspective Transformation**

Preserve x', y'
Preserve straight lines
z' independent of x, y

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![](_page_23_Picture_1.jpeg)

Preserve x', y'
Preserve straight lines
z' independent of x, y

![](_page_24_Picture_0.jpeg)

h = hither or near plane
v = projection plane

![](_page_25_Figure_0.jpeg)

1. y' = yv/z2.  $y_h' = y_hv/h$ 3.  $(v-z')/y' = v/y_h'$ 4.  $y_h/(v-h) = y/(v-z)$ 

1. y' = yv/z2.  $y_h' = y_h v/h$ 3.  $(v-z')/y' = v/y_h'$ 4.  $y_h/(v-h) = y/(v-z)$  $(v-z')/(v/z) = v/(v_h v/h)$ (v-z')/(yv/z) = v/((y(v-h)/(v-z))v/h)(v-z')/(v/z) = v/(((v-h)/(v-z))v/h)(v-z')z = vh/((v-h)/(v-z))

(v-z')z = vh/((v-h)/(v-z))(v-z')z(v-h)/(v-z) = vh(v-z')z(v-h) = vh(v-z) $v-z' \equiv vh(v-z)/z(v-h)$ z' = v - vh(v-z)/z(v-h)z' = (vz(v-h) - vh(v-z))/z(v-h) $z'z = (v^2z - vzh - v^2h + vhz)/(v-h)$  $z'z = (v^2z - v^2h)/(v-h)$  $z'z = v^2 z/(v-h) - v^2 h/(v-h)$ 

 $z'z = v^2 z/(v-h) - v^2 h/(v-h)$ In the case where v = 1 (PHIGS GL?) z'z = z/(1-h) - h/(1-h)

 $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1/(1-h) & -h/(1-h) \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$ 

![](_page_30_Figure_1.jpeg)

## Many appropriate matrices

- Similar matrices appear in many different forms
  - Different possible eye position, near plane and view plane configurations
  - some books include an additional transformation to screen coordinates
  - There is not one right answer!

![](_page_32_Picture_0.jpeg)

![](_page_33_Picture_0.jpeg)

![](_page_34_Picture_0.jpeg)

![](_page_35_Picture_0.jpeg)

![](_page_36_Picture_0.jpeg)

![](_page_37_Picture_0.jpeg)

![](_page_38_Picture_0.jpeg)

![](_page_39_Picture_0.jpeg)