# Geometry-based Modeling and Simulation of 3D Multipath Propagation Channel with Realistic Spatial Characteristics

Aleksei Fedorov, Haibo Zhang, and Yawen Chen Department of Computer Science, University of Otago, Dunedin, New Zealand, Emails: {aleksei, haibo, yawen}@cs.otago.ac.nz

Abstract—For high-resolution massive MIMO and very large antenna arrays, wireless channel models have to scrutinize the detailed space features of the surrounding environment. Existing models such as WINNER and 3GPP are not appropriate for validating and evaluating new concepts for 4G/5G as they do not consider the spatial characteristics of the real environment. The simplified 3D shapes of simulated objects in geometrybased channel models, which are constructed using vertical and horizontal planes, may cause significant difference from the real channel. In this paper, we present an approach to model the specular reflection of a signal from an arbitrary inclined surface by taking into account the signal's polarization and a spatial distribution of massive MIMO antenna elements. The approach was validated through simulating LTE uplink transmissions in an environment modeled based on Google Maps. Results showed the importance of considering detailed 3D characteristics of the surroundings in simulations. We observed that even slightly inclined walls can have significant influence on channels in comparison with models with only vertical and horizontal surfaces due to different propagation paths, different angles of reflection, and different changes of polarizations.

#### I. Introduction

The wireless signal propagation environment is very complex in terms of accurate modeling. It is a challenging task to take into account all factors such as shapes of landscapes, buildings, moving objects and trees/foliage. Even though field experiments are more appropriate for validating new concepts and approaches on wireless communication than simulation tests, field tests are commonly very expensive and time-consuming. Hence, new concepts in wireless communication are generally first validated through simulation, which demands the simulation models to be realistic enough to provide all required effects of a real propagation environment.

In the wireless communication field, the multipath propagation channel is widely used to model the signal propagation environment. It uses the ray tracing approach and takes into account physical conditions where a sent signal undergoes reflections, diffractions, and scattering from different obstacles [1]. While the multipath signal propagation enables communication when the Line-of-Sight (LoS) direction is blocked, it also has other effects including destructive and constructive interference and phase shifting of the signal. The destructive effects can have harmful impacts on the power of the received signal and make the signal undecodable due to low Signal to Noise Ratio (SNR). Hence, it is vital to develop a simulation

module that could model such effects, which in turn allows the development of efficient solutions to deal with the effects.



Fig. 1. The Gate of Europe in Madrid of Spain are twin inclined office buildings. If we have the base station (BS) and user equipment (UE) deployed as shown in the figure, the signals between these two devices can be reflected by the twin office buildings.

Existing 3-Dimensional multipath models can be generally divided into three groups: Stochastic Channel (SC) models [2] [3] [4], Geometry-based Channel (GC) models [5], and the combination of the above two [6]. The SC models have comparatively low complexity, but do not consider specific environment features, whereas a local medium is the main determining factor of a channel. Therefore, SC models are not suitable to validate new concepts such as beamforming and radio resource reuse that require specific characteristics of a local environment to deal with spatial properties of a channel. The GC models consider the impact of surrounding infrastructures, but they consider only simple shapes of objects described using vertical and horizontal planes. Meanwhile, many objects in a real environment have complex shapes with inclined surfaces (e.g. Fig 1) that can have a crucial impact on channel behavior. Consequently, the modeled channel may significantly differ from the real channel due to the inaccuracy of objects' representation. These facts motivated us to investigate new realistic models.

The goal of this paper is to examine the significance of inclined surfaces in the simulation of a radio channel. To achieve this goal, we compare the channels generated by an environment with inclined walls and an environment with vertical walls. The difference between the channels can be seen from the example shown in Fig. 2. The Base Station (BS) receives two copies of the signal from the User Equipment

(UE): one comes through LoS, and the other is reflected from the wall. Suppose, the wavelength of the signal is  $\lambda=12$  cm (the carrier's frequency  $F_c=2.6$  GHz, which is typical for LTE systems). If the lengths of the paths differ by about 6 cm or  $6+12\cdot k$  cm, where  $k\in\mathbb{Z}$ , the two copies in superposition give a strongly attenuated signal, an effect known as Deep Fading (DF). A small inclination of the wall changes the length of the reflected signal's path (dashed lines in Fig. 2). Even if the change of the length within 12 cm, it can totally change the channel from the DF to the doubling of the power of the received signal. Hence, the accurate representation of an environment is crucial for channel simulation.

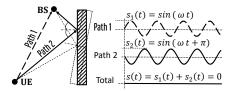


Fig. 2. The effect of DF when the reflected copies of the signal in superposition give a strongly attenuated signal regardless the power of the transmitted signal. The inclination of the wall changes the reflected path.

In this paper, we present an approach to model the reflection of signals from an arbitrary inclined surface by taking into account the polarization of signals. We incorporated Google Maps data into the simulation model and validated the necessity to consider inclined walls. The simulations show a significant difference between the channel with inclined walls and the channel with vertical walls. We implemented spherical and plane propagation waves and found that the difference between two waves is small for small antenna arrays and is significant for big antenna arrays.

# II. RELATED WORK

The 3D SC models such as WINNER [3] and 3GPP [4] were popular because they have reasonable complexity and meet the requirements of the previous communication systems such as 2G and 3G. The major drawback is that they do not deal with positions of scattering clusters but use statistical multipath parameters such as angles of arrival and departure, propagation delays, and coefficients of power attenuation. An extension of WINNER is model Quadriga [2], which is a 3D cluster-based quasi-deterministic model with the option to simulate polarization of signals. The deterministic part covers the modeling of moving UEs, and the stochastic part is mostly based on the WINNER model. However, in the case of channel evolution, the orientation of a cluster does not change appropriately regarding the movements of UE: the angle of departure for a moving UE remains unchanged, while the angle of arrival changes. This causes spatial inconsistency, which is a general problem for all existing SC models.

The channels in GC models become more spatially consistent, but they only use vertical and horizontal planes to simulate propagation effects. GEMV2 [5] simulates a channel based on information about vehicles, buildings and foliage outlines, which is taken from OpenStreetMap and traffic video records.

To avoid simulation complexity, GEMV2 works with a small area with round-trip-distance less than 500 meters. Although the simulation results are consistent with the measurements, the calculation of reflections is based on 2D map, which is fair for a flat area but not for a hilly area.

The authors of project METIS [6] experimentally evaluated that the existing models are inadequate for 5G requirements. The main drawback of the METIS model is that it is strictly limited by consideration of vertical walls, instead of inclined walls, to simulate the major interaction effects such as specular reflection and changes of polarization. Meanwhile, signal's polarization is sensitive to the parameter of inclination because the parallel and perpendicular components of polarization have different coefficients of reflection [7]. Hence, if the physical properties of materials are known, then the channel model has to scrutinize the inclination of walls to make the model more realistic and accurate.

# III. SPECULAR REFLECTION OF A SIGNAL FROM AN ARBITRARY INCLINED SURFACE

In this section, we model the specular reflection of a signal from an arbitrary inclined surface. We start the description from the consideration of a smooth surface and then extend it to a rough surface. We assume that all reflections are modeled according to the Law of Reflection and the ray tracing approach, i.e. the angle between the incident ray and the normal vector of the reflection surface is equal to the angle between the reflected ray and the normal vector, and the reflection proceeds in the plane perpendicular to the reflection surface. We do not consider reflections with two or more bounces because, in most practical cases, the energy of a transmitted signal sharply drops after the second reflection according to the Fresnel coefficients of reflection [7]. We explain our modeling using Uplink signals [8] because reflections of Uplink and Downlink signals can be modeled similarly.

#### A. Reflection from an arbitrary plane

As illustrated in Fig. 3, plane  $S_1$  is the reflection plane, plane  $S_2$  is perpendicular to  $S_1$ , and point K is the reflection point. Suppose UE is a transmitter and BS is a receiver with coordinates UE and BS, respectively.

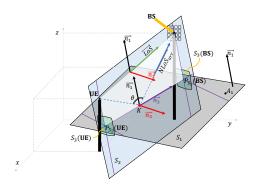


Fig. 3. Illustration of the Law of Refection.

A plane can be defined by its normal vector and a point, through which the plane goes. In the remaining sections of the paper, all normal vectors are assumed to be unit vectors. Suppose plane  $S_1$  has the normal vector  $\vec{n}_1 = (n_{11}, n_{12}, n_{13})$  and a point  $A_1 = (x_1, y_1, z_1)$ . Hence, it can be represented as follows:  $\vec{n}_1 \cdot (x, y, z) - \vec{n}_1 \cdot A_1 = 0$ . Here, the notation "·" means the dot product.

As shown in Fig. 3, the vector of Line-of-Sight can be defined as  $\overline{LoS} = (\mathbf{BS} - \mathbf{UE})/d_{LoS}$ , where  $d_{LoS} = \|\mathbf{BS} - \mathbf{UE}\|$  is the Euclidan distance between UE and BS. Since  $S_1$  and  $S_2$  are perpendicular to each other and the points  $\mathbf{UE}$ , K and  $\mathbf{BS}$  are on  $S_2$ , the normal vector  $\vec{n}_2$  of the plane  $S_2$  is the cross product of  $\overline{LoS}$  and  $\vec{n}_1$ , that is,  $\vec{n}_2 = (\overline{LoS} \times \vec{n}_1)/\|\overline{LoS} \times \vec{n}_1\|$ , and plane  $S_2$  can be represented as follows:  $\vec{n}_2 \cdot (x, y, z) - \vec{n}_2 \cdot \mathbf{UE} = 0$ .

To define the path/trajectory of the reflected signal inside  $S_2$ , we first find the intersection of planes  $S_1$  and  $S_2$ , which is the line with the direction vector  $\vec{n}_3 = \vec{n}_1 \times \vec{n}_2$ , and then find the reflection point K. We construct two planes  $S_3(\mathbf{UE})$ :  $\vec{n}_3 \cdot (x,y,z) - \vec{n}_3 \cdot \mathbf{UE} = 0$ , and  $S_3(\mathbf{BS})$ :  $\vec{n}_3 \cdot (x,y,z) - \vec{n}_3 \cdot \mathbf{BS} = 0$  that are perpendicular to both  $S_1$  and  $S_2$ . As illustrated in Fig. 3, the projections  $P_{S_1}(\mathbf{UE})$  and  $P_{S_1}(\mathbf{BS})$  of points  $\mathbf{UE}$  and  $\mathbf{BS}$  on  $S_1$  can be found as intersections of planes  $\{S_1, S_2, S_3(\mathbf{UE})\}$  and  $\{S_1, S_2, S_3(\mathbf{BS})\}$ , respectively.

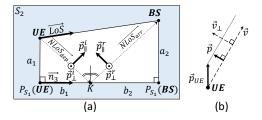


Fig. 4. (a) Reflection of the signal inside the plane  $S_2$ . (b) Polarization changes according to the observed direction.

Once  $P_{S_1}(\mathbf{UE})$  and  $P_{S_1}(\mathbf{BS})$  are defined, we can find the point K as illustrated in Fig. 4(a). The point K divides the segment  $[P_{S_1}(\mathbf{UE}), P_{S_1}(\mathbf{BS})]$  with length  $d = \|P_{S_1}(\mathbf{UE}) - P_{S_1}(\mathbf{BS})\|$  into two segments with lengths  $b_1$  and  $b_2$ . The segments  $[\mathbf{UE}, P_{S_1}(\mathbf{UE})]$  and  $[\mathbf{BS}, P_{S_1}(\mathbf{BS})]$  have lengths  $a_1 = \|\mathbf{UE} - P_{S_1}(\mathbf{UE})\|$  and  $a_2 = \|\mathbf{BS} - P_{S_1}(\mathbf{BS})\|$ , respectively. From the Law of Reflection,  $\angle P_{S_1}(\mathbf{UE})K\mathbf{UE} = \angle P_{S_1}(\mathbf{BS})K\mathbf{BS}$ , we obtain  $b_1 = a_1 \cdot C$  and  $b_2 = a_2 \cdot C$ , where  $C = d/(a_1 + a_2)$ . Finally, the coordinates of the reflection point K can be found as  $K = P_{S_1}(\mathbf{UE}) + b_1 \cdot \vec{n}_3$ .

The trajectory of the reflected signal inside  $S_2$  is defined through the arrival and departure directions, which are called as Non-Line-of-Sight (NLoS) arrival and departure, and can be computed as follows:  $\overrightarrow{NLoS_{arr}} = (\mathbf{BS} - K) / \|\mathbf{BS} - K\|$ , and  $\overrightarrow{NLoS_{dep}} = (K - \mathbf{UE}) / \|K - \mathbf{UE}\|$ , accordingly. As shown in Fig. 4(a), the total distance covered by the reflected signal is  $d_{NLoS} = \|\mathbf{BS} - K\| + \|K - \mathbf{UE}\|$ .

### B. Perpendicular and parallel components of polarization

The polarization of a signal is defined by the direction of its electric field, which is perpendicular to the direction of signal propagation [9]. The polarization of an antenna is quite a complex concept in terms of physics. Very roughly, the polarization of an antenna can be defined by the direction of its transducer element, which converts electric current to electromagnetic waves and vice-versa. We define polarizations of UE and BS antennas as unit vectors  $\vec{p}_{UE}$  and  $\vec{p}_{BS}$ , respectively. As illustrated in Fig. 4(b), if a transmitted signal is observed in direction  $\vec{v}$ , then the polarization  $\vec{p}$  of the signal is defined as projection of  $\vec{p}_{UE}$  to  $\vec{v}_{\perp}$  and calculated as follows:  $\vec{p} = (\vec{p}_{UE} \cdot \vec{v}_{\perp}) \cdot \vec{v}_{\perp}$ . The observation in direction  $\vec{v}$  causes additional attenuation of the reception. Here, vector  $\vec{v}_{\perp}$  is perpendicular to  $\vec{v}$ . Note,  $\vec{v}$  and  $\vec{v}_{\perp}$  are unit vectors.

As illustrated in Fig. 4(a) and Fig. 3, in the case of reflection, the signal interacts with plane  $S_1$  at point K and its polarization vector  $\vec{p}$  is decomposed into the perpendicular  $p_{\perp} = \vec{p} \cdot \vec{n}_2$  and parallel  $p_{\parallel} = \vec{p} \cdot (\vec{n}_2 \times NLoS_{dep})$  components relative to  $S_2$ . The decomposed components are attenuated in accordance with the Fresnel reflection coefficients  $\Gamma_{\perp}$  and  $\Gamma_{\parallel}$ , which depend on the angle of an incident ray and the material of the surface [7]. The polarization of the reflected signal is expressed as follows:  $\vec{p}_{ref} = \Gamma_{\perp} \cdot p_{\perp} \cdot \vec{n}_2 + \Gamma_{\parallel} \cdot p_{\parallel} \cdot \vec{n}_2 \times NLoS_{arr}$ . The equation shows that the reflection changes polarization of a signal, and the result of the change is inextricably linked with the value of inclination of the reflecting surface. The final attenuations caused by polarization transformations for LoS and NLoS directions can be calculated as follows:

$$G_{LoS} = \vec{p} \cdot \vec{p}_{BS}, \quad G_{NLoS} = \vec{p}_{ref} \cdot \vec{p}_{BS}.$$
 (1)

## C. Extension to a rough surface

In the case of a rough surface, the energy of the specularly reflected signal is reduced due to the scattering effect [10] [11]. The energy of the incident signal is scattered in multiple directions instead of only the direction of specular reflection. According to the Rayleigh criterion [7], a surface is considered to be rough if the difference h between the minimum and maximum heights of a surface is higher than the critical height  $h_c$  that can be calculated as follows:

$$h_c = \lambda/(8 \cdot \cos \theta),\tag{2}$$

where  $\theta$  is the angle between the incident ray and the normal vector of a surface, as shown in Fig. 3. The attenuation coefficient  $\rho_s$  caused by a rough surface is given by

$$\rho_s(\theta) = \exp\left[-8 \cdot (\pi \cdot \sigma_h \cdot \cos \theta)^2 / \lambda^2\right],\tag{3}$$

where  $\sigma_h$  is the standard deviation of the surface's height.

#### IV. SIMULATION OF MIMO ANTENNAS

In this section, we model the signal reception at the MIMO antenna side. First, we explain how to sort antenna elements according to the receiving sequence under the assumption of plane waves. Then we describe how to calculate time differences on signal reception between different antenna elements, and further extend our model to spherical waves.

As illustrated in Fig. 5(a), the antenna is deployed in a plane perpendicular to  $O_x$  axis, the normal vector of the plane is

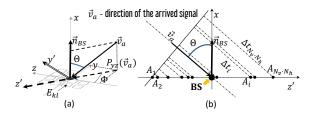


Fig. 5. (a) The geometry of an antenna array. (b) Calculation of time delays according to the receiving sequence.

denoted by  $\vec{n}_{BS}$ . We use  $\vec{v}_a$  to denote any arrived signal ( $\overrightarrow{LoS}$  or  $\overrightarrow{NLoS_{arr}}$ ). The angle between  $\vec{v}_a$  and  $\vec{n}_{BS}$  is denoted as  $\Theta$ , and the angle between axis  $O_z$  and the projection of  $\vec{v}_a$  to plane  $O_{yz}$ , which is  $P_{yz}(\vec{v}_a)$ , is denoted as  $\Phi$ . The cosines of both angles  $\Theta$  and  $\Phi$  can be calculated as follows:  $\cos\Theta = -\vec{n}_{BS} \cdot \vec{v}_a$ ,  $\cos\Phi = (\vec{e}_z \cdot P_{yz}(\vec{v}_a))/\|P_{yz}(\vec{v}_a)\|$ , where  $\vec{e}_z$  is the direction vector of the  $O_z$  axis.

#### A. Sorting antenna elements

The coordinates of the antenna elements are denoted as  $E_{kl}$   $(k=1,\ldots,N_v,l=1,\ldots,N_h)$ , where  $N_v$  and  $N_h$  are the numbers of vertical and horizontal elements. As illustrated in Fig. 5(a), signal  $\vec{v}_a$  first reaches the bottom right element and then all other elements sequentially. To know the sequence in which the elements receive the signal, we sort all elements according to their positions relative to the new axis  $O_{z'}$ , which is defined by rotating  $O_z$  with angle  $\Phi$ . Hence, to sort antenna elements according to the receiving sequence, we need to rotate the old coordinate system  $O_{yz}$  counterclockwise with angle  $\Phi$  to obtain the new coordinate system  $O_{y'z'}$ . After the rotation, coordinates in the new system can be found using the following equation:

$$\begin{pmatrix} y' \\ z' \end{pmatrix} = \begin{pmatrix} \cos \Phi & \sin \Phi \\ -\sin \Phi & \cos \Phi \end{pmatrix} \begin{pmatrix} y \\ z \end{pmatrix}.$$

As illustrated in Fig. 5(b), elements  $E_{kl}$  can be sorted in ascending order relative to z' coordinate, and the resulting set can be noted as  $A_i, i = 1, \ldots, N_v \cdot N_h$ .

# B. Calculation of time differences

As illustrated in Fig. 5(b), the signal first reaches element  $A_1$ , then  $A_2$ , etc. We use  $d_{12}$  to denote the Euclidian distance between elements  $A_1$  and  $A_2$  in z' coordinates. To reach element  $A_2$  after  $A_1$ , the arrived signal spends time  $\Delta t_2$ , which can be calculated as:  $\Delta t_2 = d_{12} \cdot \sin \Theta/c$ , where c is the speed of light. Hence, the time it takes for the signal to reach point  $A_i$  can be calculated as  $\Delta t_i = d_{1i} \cdot \sin \Theta/c$ , where  $d_{1i}$  is Euclidian distance between  $A_1$  and  $A_i$  in z' coordinates.

# C. Extension to spherical waves

For spherical waves [6], each element of the antenna has its own LoS and NLoS directions. Thus, the calculation of the directions should be performed separately for each element, i.e. all steps from section III should be done for each element. This approach, obviously, increases the computational complexity of the simulation, but this increase is not critical in comparison with the processing complexity of received signals.

#### V. SIMULATIONS

To validate our solution in terms of modeling reflections from an arbitrary surface, we implemented a simulation model in MATLAB and simulated LTE Uplink transmissions.

#### A. Simulation setup

The carrier's frequency  $F_c$  is set to 2.6 GHz, which is typical for LTE systems. In order to examine the channel behavior on the whole bandwidth of Uplink, we allocated the maximum bandwidth in 100 Resource Blocks (RB) to one UE, where each RB has 12 subcarriers with each having a bandwidth of 15 kHz [8]. The simulation includes one UE and one BS. The UE has only one antenna element, whereas the number of antenna elements in BS is varied from 1 to 100. Each element receives a multipath signal mixed with additive white Gaussian noise with 15 dB of SNR. The distance between elements on the antenna array is configured to be half of the wavelength  $\Delta d = \lambda/2 \approx 6$  cm [9]. The BS has vertical polarization  $\vec{p}_{BS}$ , while the polarization  $\vec{p}_{UE}$  for UE can be configured with three options: (1) Horizontal, (2) Vertical, and (3) Inclined with 45-degree polarization.

1) Environment setup: As shown in Fig. 6, we construct the environment model based on the area of the Gate of Europe in Spain obtained from Google Maps (Fig. 1). The geometrical characteristics of the buildings are obtained from the website [12]. The height of the buildings is 114 meters, and the angle of inclination is 15 degrees for both towers. In our setup, the height of BS antenna is 30 meters, and UE is 1.9 meters.

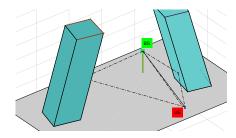


Fig. 6. The model of the Gate of Europe. Solid line is the LoS, and dashdoted lines represent reflections from inclined walls.

In order to evaluate the influence of inclined surfaces and spherical waves to channel generation, we examine both types of waves (plane and spherical) and use the following three environment setups: (1) *Inclined walls* (the real inclination of towers with 15 degrees), (2) *Vertical walls* (no inclination for the two towers), and (3) *Displaced walls* (the inclination degree is set to 1°). Fig. 6 shows both the LoS path and the NLoS paths due to reflections from inclined walls.

2) The effect of wall roughness: Based on the street view from Google Maps, it can be seen that the majority of the surface of the buildings is covered by a glass material and the floor under the UE is made from concrete. As illustrated in Fig. 1, the gray straight elements on the buildings make the walls rough. We assume that the gray elements stick out from the main surface with  $h_{\rm max}=0.2$  meters, which is higher than the critical value of the roughness  $h_c$  given in Eq. (2) for

all angles of incidence  $\theta$  from  $0^{\circ}$  to  $86^{\circ}$ . In our simulation, angles of reflection are smaller than  $86^{\circ}$ . Hence, the walls are considered as rough, and the attenuation coefficient given in Eq. (3) is used. From the street view, we roughly estimate the percentage of gray elements as 25% of the surface, which results in standard deviation  $\sigma_h = 0.08$  m.

3) Calculation of reflection and penetration coefficients: All the physical parameters of materials and the equations used for calculating the Fresnel coefficients of reflection are used in accordance to the METIS report [6], and set as follows: (1) Glass material: relative permittivity  $\varepsilon_r' = 7.0$ , and conductivity  $\sigma = 0.25$ ; (2) Concrete material:  $\varepsilon_r' = 5.31$ , and  $\sigma = 0.0707$ . The perpendicular and parallel Fresnel coefficients are calculated as follows:

$$\Gamma_{\perp}(\theta) = \frac{\cos \theta - \eta}{\cos \theta + \eta}, \quad \Gamma_{\parallel}(\theta) = \frac{\varepsilon_r \cdot \cos \theta - \eta}{\varepsilon_r \cdot \cos \theta + \eta},$$
 (4)

where  $\eta = \sqrt{\varepsilon_r - \sin^2 \theta}$ ,  $\varepsilon_r = \varepsilon_r' - j \cdot 17.98 \cdot \sigma/f$ , j is the imaginary unit, and f is the frequency in GHz. We use f = 2.6 in our simulation.

Our aim is to examine the reflection impact on the channel. Therefore, we assume that LoS direction and the signals reflected from the concrete floor are blocked by human. The physical parameters of a human's body are:  $\varepsilon_r' = 2.97$  and  $\sigma = 0.0116 \cdot f^{0.7076}$ . The penetration coefficient through a human body is calculated as follows:

$$T_h = \frac{(1 - \Gamma_h^2) \cdot \exp(-j \cdot (\delta - \frac{2\pi}{\lambda} \cdot d_h))}{1 - \Gamma_h^2 \cdot \exp(-j2\delta)},\tag{5}$$

where  $\delta = \frac{2\pi}{\lambda} \cdot \sqrt{\varepsilon_r}$ ,  $d_h$  is the thickness of the human's body (0.6 m in our simulation), and  $\Gamma_h$  means Fresnel coefficient for the perpendicular and parallel components of a signal, which are calculated based on Eqs. (4). In the case of human body penetration, we assume that the antenna of UE is close enough to a human's body, i.e.,  $\theta = 0$ .

4) Free space pathloss and attenuation coefficients: As our aim is to examine the effect of reflection, we use the following simple model of free space path loss  $PL(d) = \lambda^2/(4\pi d)^2$ , where d is the distance covered by a signal. The attenuation coefficients for each propagation path are calculated separately as follows based on Eqs. (1), (3), (5): for the LoS path  $K_{LoS} = G_{LoS} \cdot T_h \cdot PL(d_{LoS})$ , for the reflected from the floor NLoS path  $K_{floor} = G_{NLoS}^{concrete} \cdot T_h \cdot PL(d_{NLoS})$ , and for reflected from walls NLoS paths  $K_{NLoS} = \rho_s \cdot G_{NLoS}^{glass} \cdot PL(d_{NLoS})$ . Here,  $G_{NLoS}^{material}$  is the attenuation coefficient caused by polarization change in dependency to the material.

#### B. Simulation Results

In this section, we present the results of channel response based on LTE Uplink channel estimation (CE) procedure [8]. The receiver sums up signals from antenna elements together and feeds the total signal to the CE procedure. As the channel measurements are noisy, we average the measurements using a sliding window with length of 10 samples. All graphs in Fig. 7 and Fig. 8 represent the results of CE of one LTE slot [8].

1) Scenario I (one reflecting surface): To evaluate the correctness of the simulation approach, we first run the simulation in a simple scenario with one reflecting surface, which is the concrete floor. By intuition, it is anticipated that the power of the received signal should be higher if the antennas (UE and BS) have the same polarization and should be lower when the polarizations are perpendicular to each other. For 45 degrees of difference in polarizations, the resulting channel response should be between the two channel responses for vertical and horizontal. As illustrated in Fig. 7, this intuition is well justified: black lines represent the situation when both antennas have the same polarizations, blue lines represent the situation when the polarization of UE is inclined on 45 degrees relative to the vertical axis, and red lines represent the situation when the polarization of UE is horizontal. This indicates that, by changing the receiver's/transmitter's polarization, the connection quality can be improved. Since the UE is not located in the direction perpendicular to the antenna panel of the BS, the polarization of the transmitted signal is changing through LoS and NLoS paths. Hence, the BS can receive nonzero signals from UE when it has horizontal polarization.

In this simulation, it can be observed that the larger the number of antenna elements at the BS, the stronger the received signal strength, which is consistent with ideal MIMO situations. Another observation is that the discrepancy between channels generated based on plane waves and spherical waves grows with the number of antenna elements. This is caused by the fact that the maximum distance between two antenna elements increases with the increase of the number of antenna elements. When the number of elements is small, spherical waves can be accurately approximated by plane waves because the difference between these waves is minuscule. However, for an antenna with a large number of elements, the difference in receiving signal power for elements that are far away from each other is large. Hence, the approximation of spherical waves by plane waves becomes rough, which has big influences on the generation of a channel. This effect is well observed in Fig. 7: for four antenna elements, the spherical and plane channels are very close; for 16 elements the channels begin to differ and the discrepancy becomes significant for 100 elements. For example, in this particular scenario, the average difference is about 1 dB, and for other scenarios with multiple reflecting surfaces the difference could be even larger.

2) Scenario II (the Gate of Europe): The main aim of this scenario is to show the importance of considering inclined surfaces in simulations. We compare channel responses in the three setups given in Section V-A1. The displaced walls are simulated to show that even a small inclination can have a significant impact on channel behavior. The polarization of BS antenna is vertical, and the UE has 45-degree polarization.

In Fig. 8, black lines represent the model with inclined walls, blue lines represent the model with vertical walls, and the red lines represent displaced walls. Thin lines mean that channels are generated by spherical waves, and thick lines mean the channels are generated by plane waves. For the sake of simplicity, we call them as spherical channels and plane

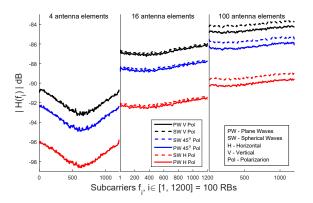


Fig. 7. Impact of polarization, different types of waves, and different number of antenna elements at BS: the polarization  $\vec{p}_{UE}$  of UE has three states: V, H and 45°. The number of BS antenna elements varies between 4, 16 and 100 elements with all elements having vertical polarization.

channels, respectively. As shown in Scenario I, the difference between channels generated by spherical and plane waves is small when the number of antenna elements is small. It can be seen from Fig. 8 that, for four antenna elements, the difference between spherical and plane channels is less than 0.3 dB. Moreover, all three models generate channels close to each other, and the maximum discrepancy is less than 1.4 dB. It indicates that it is feasible to use plane waves to simulate multipath channels for small antenna arrays.

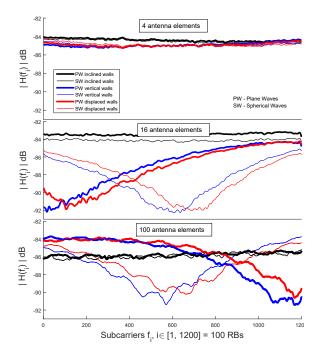


Fig. 8. Impact of number of antenna elements and different types of waves in the Gate of Europe scenario. The BS has vertical polarization, and the UE has  $45^{\circ}$  polarization. The number of antenna elements varies between 4, 16 and 100.

With the increase of the number of antenna elements, the difference between generated channels becomes significant.

For 16 elements, the maximum difference between the channels with inclined walls and with vertical walls is around 8 dB. The models with vertical and displaced walls generate similar channels, and the difference between them is less than 2 dB. An interesting observation is that the spherical channel and the plane channel are very close in the model with inclined walls, while they are significantly different in the other models. For example, the difference for inclined walls is less than 1 dB, while the difference for vertical/displaced walls is up to 6 dB. In the case of 100 elements, channels with vertical walls and displaced walls start to differ up to 3 dB, which can be vital for the LTE procedures such as signal equalization, demodulation, decoding. These results indicate that a system with large antenna arrays (e.g. massive MIMO systems) will become more sensitive to the accurate environment representation and will need very accurate channel models.

#### VI. CONCLUSION

In this paper, we opened the problem of accurate representation of an environment in the wireless channel simulation. In the case of signal reflection, we closed the problem by proving that the parameter of inclination has a big impact on channel modeling. The further development of this research lays in the experimental validation of the proposed approach and enhancement of the simulation scenario by the calculation of channel responses for all potential positions of BS and UE.

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